THE METRIC THEORY OF TEICHMÜLLER SPACES OF COMPACT RIEMANN SURFACES:
(A COURSE AT THE MORNINGSIDE CENTER OF MATHEMATICS, BEIJING, MARCH 2019)

ATHANASE PAPADOPOULOS

In this course, I will give an introduction to the Teichmüller and the Thurston metrics on the Teichmüller spaces of compact surfaces, with a stress on the comparison between the two metrics.

The outline is the following:

1: The Teichmüller metric: Definition and main properties.

2: The Thurston metric and the arc metric: Definitions and main properties.

3: Geodesics and anti-geodesics.

4: The Finsler structure.

5: Mapping class group actions.

References

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